



Department of  
Mathematical Sciences

# Dissertation Defense

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Wednesday  
April 26  
EMS Building  
Room E495  
3:30pm



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## Cocompact Cubulations of Mixed 3-manifolds

Geometric group theory studies the connections between the algebraic properties of a group and the topological and geometric properties of spaces on which the group acts. If  $G$  is the fundamental group of a 3-manifold  $M$ , then  $G$  acts on the universal cover of  $M$ , but maybe we can learn more about  $G$  by studying an action on another space with a nice combinatorial structure.

Learning more about the group can also tell us more about the space. Recently, two big conjectures for hyperbolic 3-manifolds, the virtual Haken and virtual fibering conjectures, were resolved by showing that hyperbolic 3-manifolds are virtually compact special, meaning they act properly, cocompactly, and in a “special” way on a CAT(0) cube complex, proved by Wise and Agol in the cusped hyperbolic and closed cases respectively.

A natural outgrowth of this breakthrough is the goal of classifying which 3-manifold groups are virtually compact special, which was known in every case except the case of mixed manifold groups. A mixed manifold is an aspherical 3-manifold which can be cut along embedded tori, called JSJ tori, so that each component, or block, of the cut open space admits either a hyperbolic geometric structure or admits the structures of a Seifert fibered space. In this defense, we will discuss the main result of my dissertation proves that the fundamental group of a mixed manifold  $M$  is virtually compact special iff  $M$  is chargeless, meaning that interior Seifert fibered block in the JSJ decomposition of  $M$  has a trivial euler number relative to the fibers of adjacent Seifert fibered blocks.



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