

# Ph.D. Qualifying Exam

February 4th, 2016

1:00-5:00pm

## Electrical Engineering

### Part I

#### Instructions:

This is a closed-book/closed-notes exam module, four hours in duration. There are ten (10) problems in this exam, and you will have a choice of answering **only eight (8)**. **The 4 questions from EE 234 and EE310 are required.** The other 4 questions can be selected from other topics. The selected eight (8) questions must be **clearly marked** in the selection boxes below.

Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8
EE 234	EE 234	EE310	EE 310				

Write your name and student ID below.

**Full Name:** \_\_\_\_\_

**Student ID:** \_\_\_\_\_

Please write your student ID Number of **EVERY PAGE**, but **DO NOT** write your name on any other pages of the exam.

Blank paper is provided if you need additional space to show your work. **PLEASE INDICATE THE PROBLEM NUMER ON EACH ADDITIONAL PAGE YOU USE.**

Good Luck!

Final grade for this question: \_\_\_\_\_ out of 10 Points

## Question 1, ElecEng 234

### Part I EE234

a) Consider the following nonhomogeneous ODEs, find their homogeneous solution, and give the form (**no need to determine coefficients**) of nonhomogeneous solution. (40 points)

i)  $4y'' + 20y' + 29y = 3x^2 \cosh(2.5x)$

ii)  $y'' + 3y' = 2 + 5\sinh(3x)$

b) Find the general solution of  $y'' + E^2y = 2\sin(Ex)$  where E is a non-zero real constant with following steps i) Determine homogeneous solution, ii) Find nonhomogeneous solution **with coefficients determined using method of undetermined coefficients** and iii) Arrive at the general solution. (60 points)

Final grade for this question: \_\_\_\_\_ out of 10 Points

## Question 2, ElecEng 234

Consider the following matrix:

$$\begin{pmatrix} 3 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 3 \end{pmatrix}$$

- a) Find its characteristic equation. (10 points)
- b) Find all eigenvalues and the spectral radius of the matrix. (20 points)
- c) Find all eigenvectors and the geometric multiplicity of each eigenvalue. (70 points)

Final grade for this question: \_\_\_\_\_ out of 10 Points

### Question 3, ElecEng 310

(a) Using time-domain transform, find the zero-state response of an LTI Digital system:

$$y[n + 2] - 0.6y[n + 1] - 0.16y[n] = 5x[n + 2]$$

for the input  $x[n] = (4)^{-n}u[n]$ . (7 points)

(b) Given the two systems connected in series as

$x[n] \rightarrow h_1[n] \rightarrow w[n]$ , where  $w[n] = 3x[n] - 2x[n - 2]$  and,

$w[n] \rightarrow h_2[n] \rightarrow y[n]$ , where  $y[n] = 2w[n] - 3w[n - 1] - 4w[n - 2]$ ,

compute the overall impulse response, i.e.,  $x[n] \rightarrow h[n] \rightarrow y[n]$ , what is  $h[n]$ ? (3 points).

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## Question 4, ElecEng 310

(a) For the system described by the differential equation (2), find the zero-state unit step response of its inverse system, so that the cascade system of the system and its inverse system is an identity system:

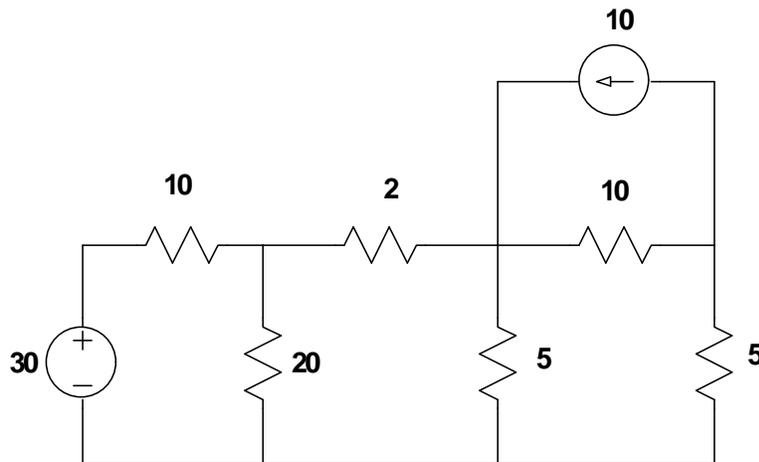
$$\frac{d^2y(t)}{dt^2} - 2\frac{dy(t)}{dt} - 3y(t) = \frac{d^2x(t)}{dt^2} - 2\frac{dx(t)}{dt} - 8x(t)$$

Final grade for this question: \_\_\_\_\_ out of 10 Points

## Question 5, ElecEng 301

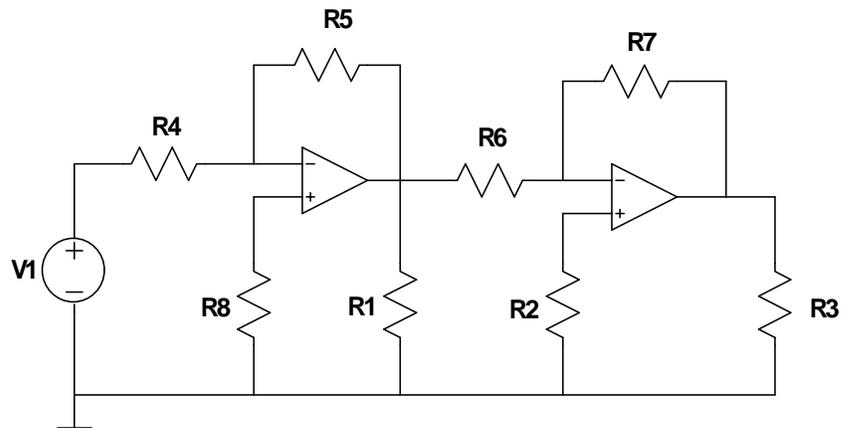
For the circuit shown below,

- Determine the Thévenin equivalent circuit seen by the 2 ohm resistor.
- Using the Thévenin equivalent circuit, determine the power absorbed by the 2 ohm resistor.
- What value of resistance should replace the 2 ohm resistor if we desire maximum power to be delivered from the circuit to the resistor?



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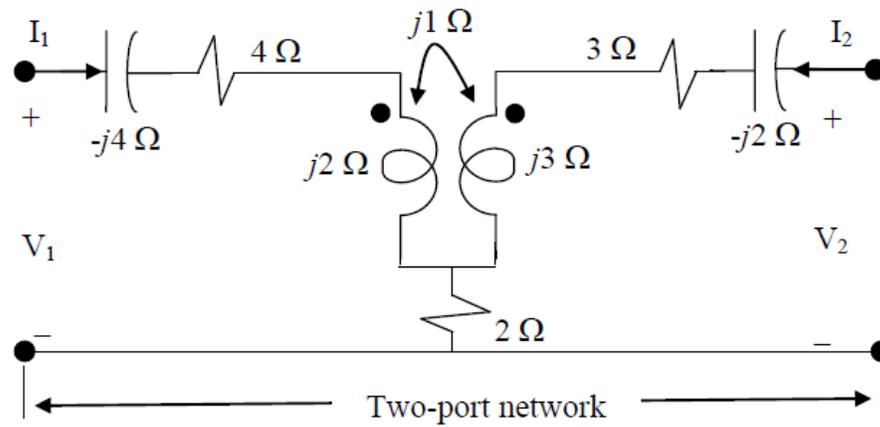
2. a) Determine the voltages across the resistors  $R_6$  and  $R_7$  (indicate the polarity for your answer).  
b) Repeat (a) if the resistor  $R_7$  is replaced by a capacitor.



Final grade for this question: \_\_\_\_\_ out of 10 Points

### Question 6, ElecEng 305

**Problem :** Determine Transmission parameters of the following two-port network.



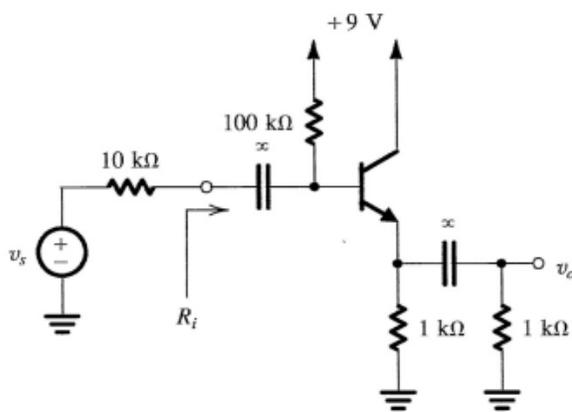
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Final grade for this question: \_\_\_\_\_ out of 10 Points

## Question 7, ElecEng 330

For the emitter follower circuit shown below, the BJT used is specified to have  $\beta$  values in the range of 30 to 300. For the two extreme values of  $\beta$  ( $\beta=30$  and  $\beta=300$ ), find:

- (a)  $I_E$ ,  $V_E$  and  $V_B$ . (5 points)
- (b) The input resistance  $R_i$ . (2 points)
- (c) The voltage gain  $v_o/v_s$ . (3 points)

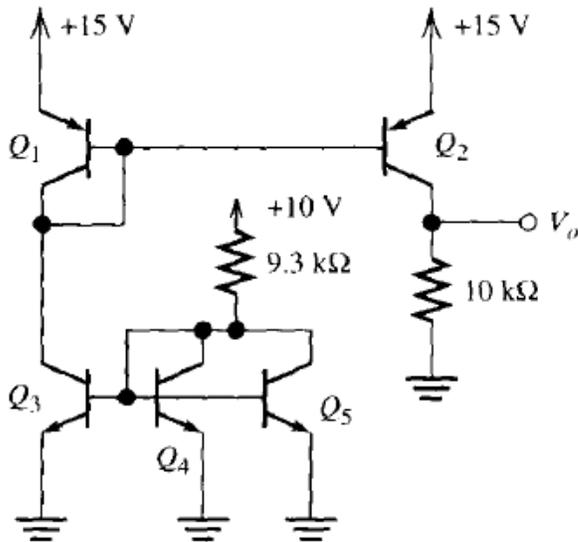


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### Question 8, ElecEng 335

Determine the collector currents of all of the transistors and the value of  $V_o$  in circuits shown below. Assume that the transistors have equal areas and are matched. Furthermore, assume that  $|V_{BE}| = 0.7\text{ V}$ , Transistor output resistance is  $\infty$ , and the base current can be neglected.



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## Question 9, ElecEng 354

- a) Design a 2 X 4 decoder. Give its truth table, a Boolean expression for each output, and its logic circuit.
- b) Design a 3 X 8 decoder using two 2 X 4 decoders.
- c) Implement function  $F = X + Y.Z$  using:
  - c1) AND, OR, and NOT gates.
  - c2) Using a decoder

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## Question 10, ElecEng 367

A. How many bytes of memory can be addressed by a microprocessor with a 16-bit address bus ?

B. Make each of the number conversions

**Example:** Convert decimal number 237 to binary.

**Answer:**  $237 = 128 + 64 + 32 + 8 + 4 + 1$ , so the binary number is %11101101

1. Convert decimal number 177 to binary.
2. Convert hexadecimal number \$2A52 to binary.
3. Convert binary number %1010 0011 to hexadecimal.
4. Convert hexadecimal number \$B7 to decimal.

C. An assembly language code segment from a typical microprocessor is shown below:

```
1. ADDA #1           ;; Add 1 to register A
2. JSR $1234         ;; Jump to a sub routine at address $1234
3. PUSH B           ;; Push the contents of register B
4. JMP $1234         ;; Jump to address $1234
5. RTS              ;; Return from a subroutine
```

1. Which instructions modify the stack ?

(Circle all that apply)    1    2    3    4    5

2. Which instructions modify the program counter ?

(Circle all that apply)    1    2    3    4    5

3. Which instructions modify data in a processor data register ?

(Circle all that apply)    1    2    3    4    5

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**D. Logic Functions in a microcomputer.**

- Match each logic device with a function (choose the best answer, indicate only one letter in each blank provided).

Logic Devices: (Indicate Function)

- |       |                                    |       |             |
|-------|------------------------------------|-------|-------------|
| _____ | 1) D Flip Flops                    | _____ | 4) Decoder  |
| _____ | 2) Logic Gates, such as AND and OR | _____ | 5) Register |
| _____ | 3) Tri-State buffer                |       |             |

Functions:

- a) Build a register
- b) Reverse the flow of data for reverse polish computation
- c) Build a circuit to perform addition in an Arithmetic Logic Unit
- d) A device in which to store a word of data in a processor
- e) Provide power
- f) Select one of several devices to activate, based on an address
- g) Connect devices to a data bus
- h) Provide timing information and device synchronization

**E. Essay Questions.** Answer each of these questions with one or a few complete sentences. Incomplete sentences will count against the grade.

1. Why do microprocessors incorporate buses ?

2. Name at least 2 kinds of buses commonly used in computers and write one or a few sentences describing each.

3. What is bus contention ?

Final grade for this question: \_\_\_\_\_ out of 10 Points

## Question 11, ElecEng 361

Problem 1. Circle only one correct answer for any 5 out of 7 questions below. Each correct answer gives 20 pt, incorrect answer gives 0 pt.

1. Consider a infinite cylindrical wire with radius  $r_0$  carrying current  $I_0$  ; assuming that current density is constant, the strength of magnetic field produced by the wire is to
  - a) increase linearly with  $r$  for  $r < r_0$
  - b) decrease as  $\sim 1/r$  for  $r < r_0$
  - c) decrease as  $\sim 1/r^2$  for  $r > r_0$
  - d) decrease as  $\sim 1/r^3$  for  $r > r_0$
  - e) increase as  $\sim r^2$  for  $r < r_0$
  - f) none of the above
  
2. A plane EM -wave travels in a free space along  $x$ -direction. The  $\vec{H}$ -vector associated with the wave is most likely given by the following equation
  - a)  $\vec{H} = 0.1\cos(10^{10}t - 133z) \hat{x}$
  - b)  $\vec{H} = 3\cos(10^{10}t - 133x) \hat{z}$
  - c)  $\vec{H} = \cos(10^{10}t - 133x) \hat{x}$
  - d)  $\vec{H} = \cos(10^{10}t - 133y) \hat{x}$
  - e)  $\vec{H} = 10\cos(10^{10}t - 133y) \hat{z}$
  
3. A proton of a constant velocity  $\vec{u}_0 = u_x\hat{x} + u_y\hat{y} + u_z\hat{z}$  enters a region of a constant magnetic field,  $\vec{B}_0 = B_0\hat{x}$ . The trajectory of the proton in the region will be
  - a) straight line
  - b) circle
  - c) solenoid-like
  - d) sinusoid
  - e) parabola
  - f) none of the above
  
4. In electrostatics, the following remains true
  - a) gravitational forces are neglected
  - b) the net charge of the system is conserved
  - c) electric field is to be produced by both polarized and free charges
  - d) both a) and b)
  - e) both b) and c)
  - f) all of the above
  
5. In magnetostatics a magnetization vector,  $\vec{M}$  was introduced. This vector
  - a) gives a magnetic dipole moment of unit volume of magnetic material
  - b) is a analog of  $\vec{P}$ -vector in electrostatics
  - c) for a magnetized Fe-bar,  $M \approx 0$
  - d) both a) and b)
  - e) both b) and c)
  - f) all of the above

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6. Consider a system of  $N$  charges, with a net charge  $Q = \sum_{i=1}^N q_i = 0$ . The following is true.
- a) the system can generate a non-zero electrostatic potential,  $V$
  - b) the dipole moment of the system is always zero.
  - c) the system can generate a non-zero electric field
  - d) both a) and b)
  - e) both a) and c)
  - f) all of the above
7. For charge continuity equation, the following is not true.
- a) The equation represents a charge conservation law stated in integral form
  - b) Recombination-generation processes are not considered as a part of derivation
  - c) The equation is used to find the relaxation time constant of an electrostatic system
  - d) both a) and b)
  - e) both b) and c)
  - f) none of the above

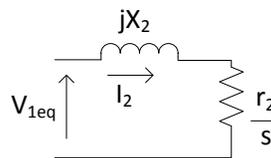
Problem 2.

Two spherical surfaces of radii  $R=a$  and  $R=b$  ( $>a$ ) carry surface charged densities of  $\rho_{sa}$  and  $\rho_{sb}$ , respectively. Find  $\vec{E}$  everywhere and the relation between  $\mathbf{a}$  and  $\mathbf{b}$  so that electric field,  $\vec{E}$  vanishes at  $R > b$  region.

Final grade for this question: \_\_\_\_\_ out of 10 Points

## Question 12, ElecEng 362

1. **Machine Overview.** Please answer the following questions. Note: this is to test your comprehension of the basic concepts. One to three word answers are sufficient.
  - a. For a DC machine and Synchronous Machine:
    - i. Name the two winding **types**
    - ii. For the DC machine, identify which type of winding is used to control torque
    - iii. Of the two machine types, which has its field on the stator?
    - iv. Which machine type uses commutator and brushes to get DC current into the rotor?
    - v. Which machine type uses slip rings and brushes to get DC current into the rotor?
    - vi. Which machine type has a magnetomotive force (mmf) that is fixed in space as the rotor is turning?
  - b. The general expression for torque in an induction machine is  $T = -K \cdot I_r \sin(\delta_r)$ . For an induction motor, it can be shown that  $\delta_r = -(90^\circ + \phi_2)$  where  $\phi_2$  is the power factor looking into the rotor circuit from the air gap (see the circuit below).



Assume that the controls to the induction motor can “effectively” change what the circuit parameters are (yes this is possible). Since the slip has to be non-zero to produce torque what would  $X_2$  have to be changed to in order to ensure **maximum torque per ampere**?

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